

Regents Park Publishers

Data Analytics



T1LM3

Excel Tutorials



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Axioms

Axioms

An **Axiom** is a mathematical statement that is **assumed** to be true.

- a self-evident truth that requires no proof
- a universally accepted principle or rule
- a proposition that is assumed without proof for the sake of studying the consequences that follow from it
- Formulas that we use are based on axioms

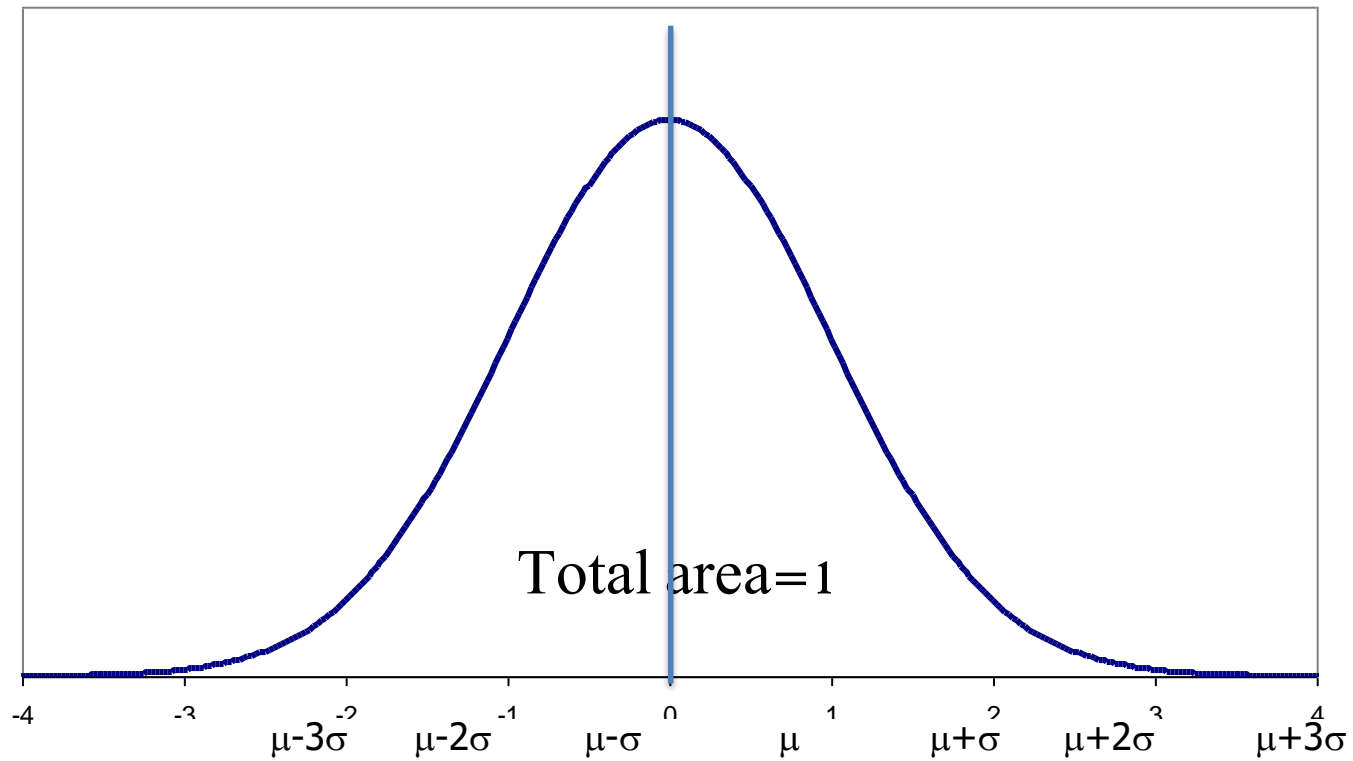


Normal Probability Distribution

Introduction

- The Normal (or Gaussian) distribution is probably the most used (and abused) distribution in statistics.
- Normal random variables are **continuous** (they can take any value on the real line) so the Normal distribution is an example of a **continuous probability distribution**.

The Normal Distribution



The graph of the normal distribution is called the normal (or bell) curve.

The Normal Distribution

- The mean, median, and mode are the same.
- The normal curve is symmetric about its mean.
- The total area under the normal curve is one.
- The normal curve approaches, but never touches, the x-axis.

Normal Distributions and Probability

- We do not talk about the probability $P[X=x]$ for continuous random variables. Rather we talk about the probability that the random variable falls in an interval, i.e. $P[x_1 \leq X \leq x_2]$.
- $P[x_1 \leq X \leq x_2]$ can be determined by finding the area under the normal curve between x_1 and x_2 .

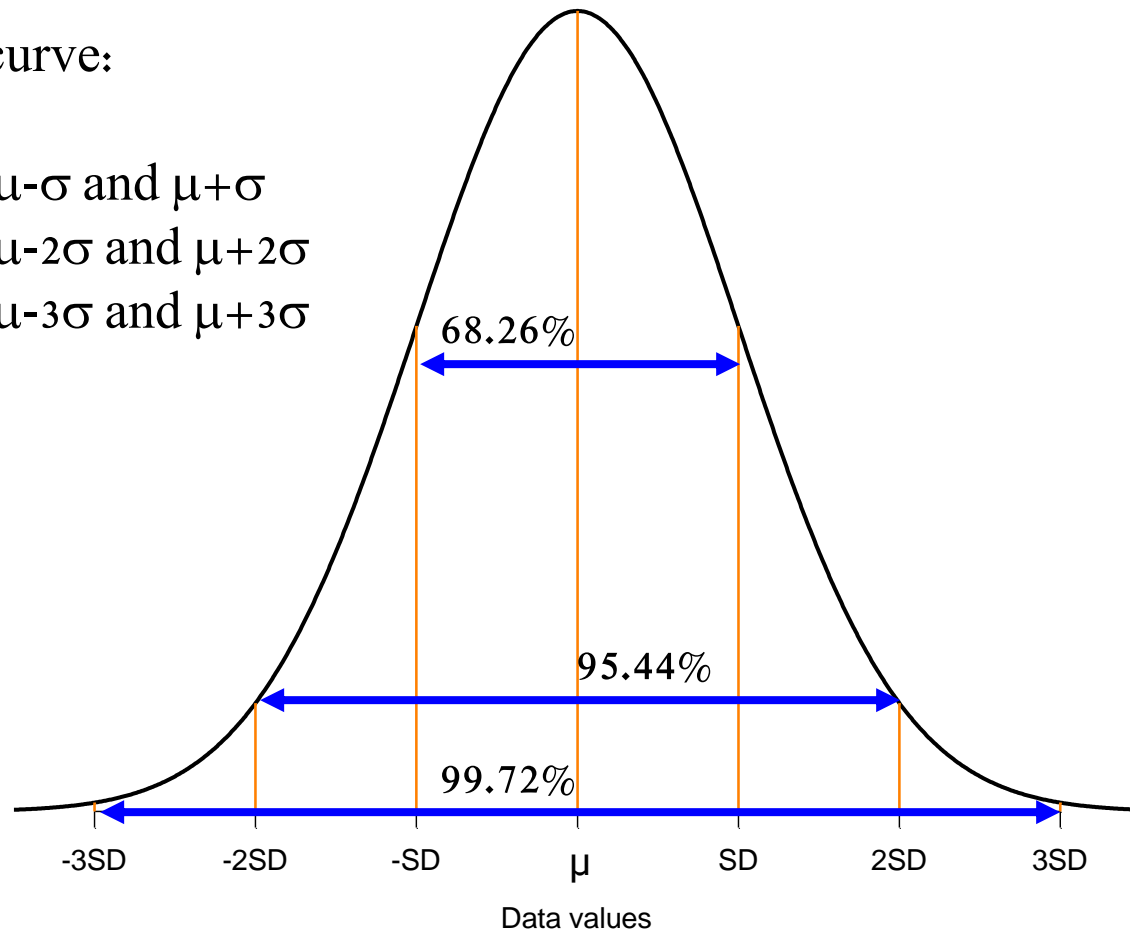
Normal Distributions and Probability

The areas under the curve:

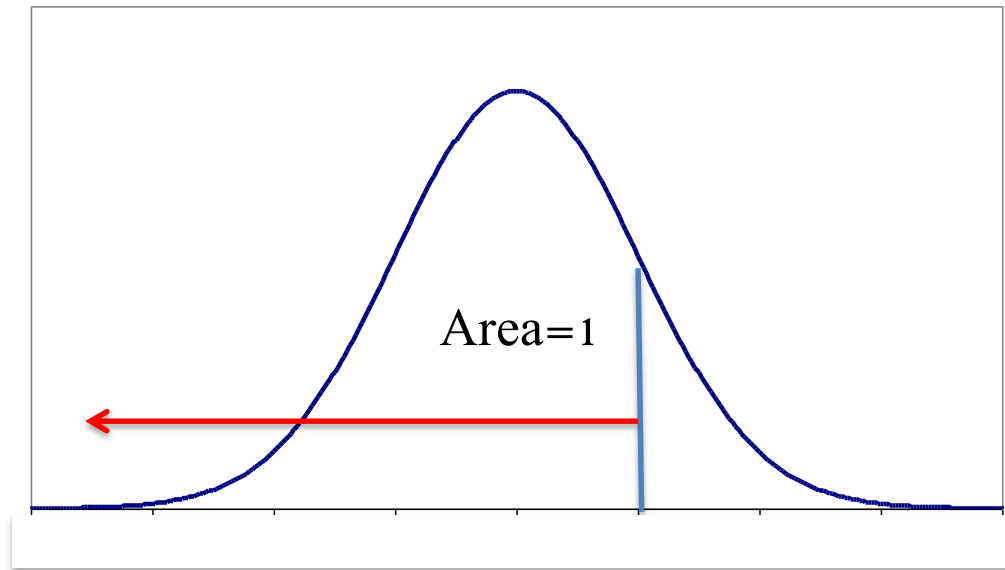
68.26% lies between $\mu - \sigma$ and $\mu + \sigma$

95.44% lies between $\mu - 2\sigma$ and $\mu + 2\sigma$

99.72% lies between $\mu - 3\sigma$ and $\mu + 3\sigma$

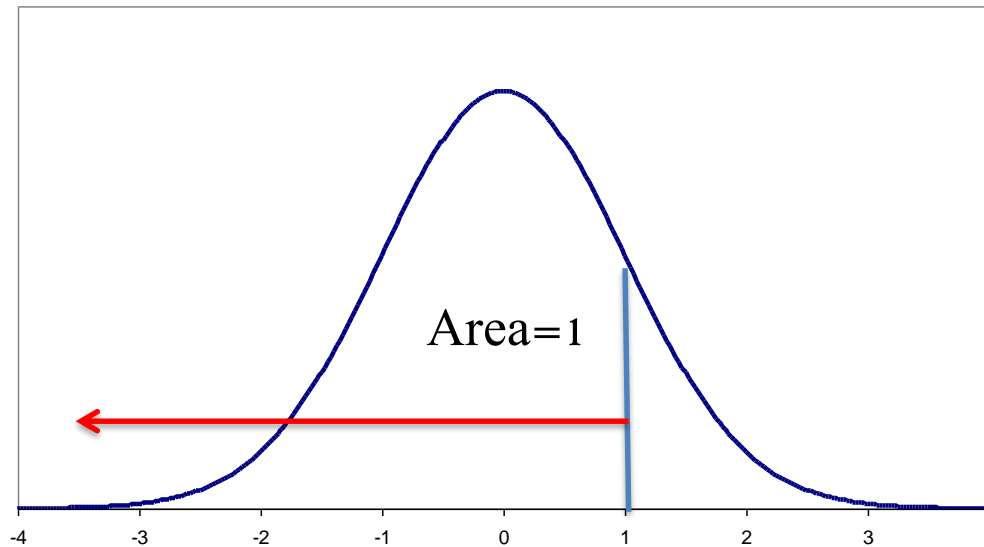


Excel Function



The area under the normal distribution from x to $-\infty$ can be computed using the EXCEL function **NORMDIST**

Excel Function



The area under the **standard** normal distribution from x to $-\infty$ can be computed using the EXCEL function **NORMSDIST**

Examples 1-3

Example 1

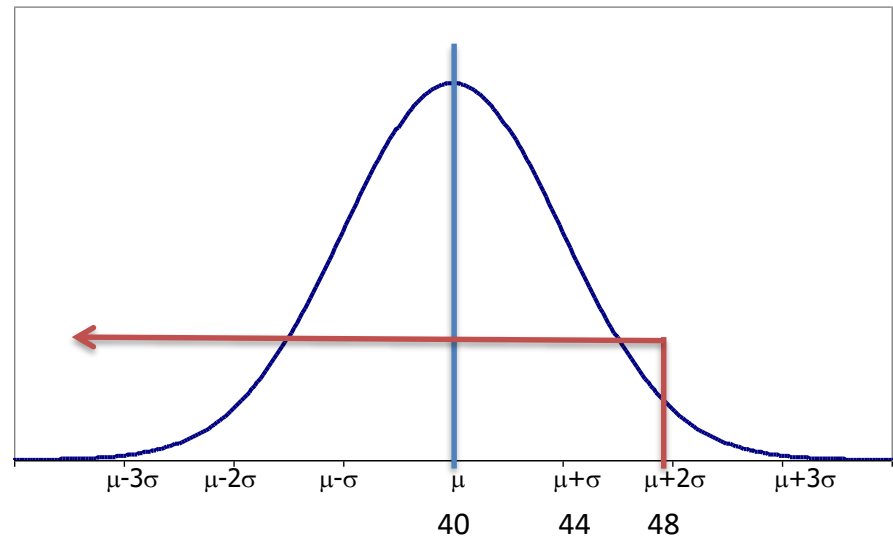
- The mean length of a fish is 40cm and the standard deviation is 4 cm. What is the probability that the length of a randomly selected fish is less than 48cm?
- 48cm is two standard deviations above the mean so the area to the left of 48cm is

$$0.5 + 0.475 = \mathbf{0.9772}$$

or

$$\mathbf{NORMDIST(48,40,4,1)=}$$

$$\mathbf{0.9772}$$



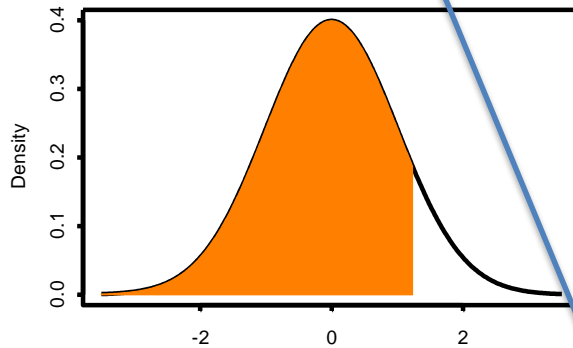
Example-2

- Find the area under the normal distribution curve between -0.12 and 1.23.
 - We use our previous approach:
 - $P[-0.12 \leq X \leq 1.23] = P[X \leq 1.23] - P[X \leq -0.12]$
 - In EXCEL:
 - $\text{NORMDIST}(1.23,0,1,1) - \text{NORMDIST}(-0.12,0,1,1)$

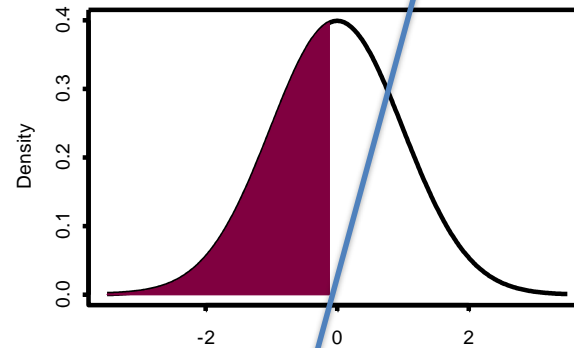
$\text{NORMDIST}(x, \mu, \sigma, 1)$

Example-3

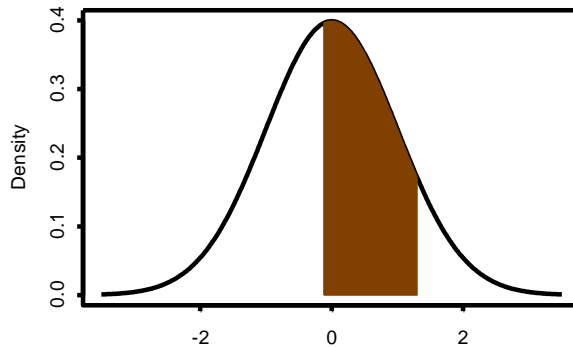
$$P[X \leq 1.23] = 0.8907$$



$$P[X \leq -0.12] = 0.4522$$



$$P[X \leq 1.23] - P[X \leq -0.12] =$$



$$0.8907 - 0.4522 = 0.4384$$



Standardized Normal Probability Distribution

The Standard Normal Distribution

The normal distribution with a mean of 0 and a standard deviation of 1 is called the

Standard Normal Distribution

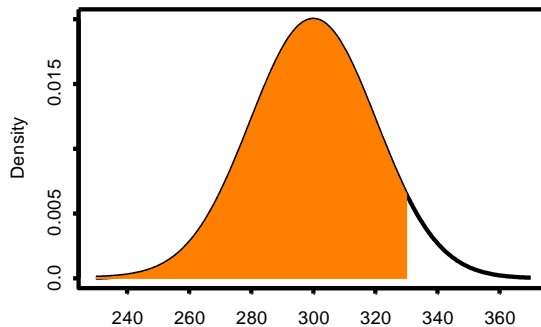
- The standard normal distribution and the z-score:

$$z = \frac{\text{value} - \text{mean}}{\text{standard deviation}} = \frac{x - \mu}{\sigma}$$

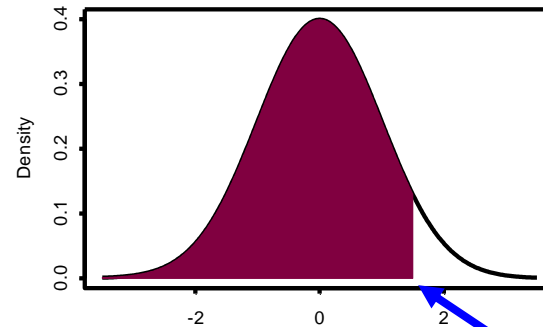
Standardization

- We can transform any normal distribution into a standard normal distribution by subtracting the mean and dividing by the standard deviation.

$\mu=300; \sigma=20; X=330$



$\mu=0; \sigma=1; Z=1.5$



Area=0.933 in both cases

$$Z = (x-300)/20$$

Standardization

- To find the probability that $X \leq Y$ if X is normally distributed with mean μ and standard deviation σ .
 - Compute the z-score: $z = (y - \mu) / \sigma$
 - Calculate the area under the normal curve between $-\infty$ and z
 - We could calculate this area directly using the EXCEL function:

Standardize

Examples 1-3

Examples 1-3

- The average swimming speed of a fish population is 2 m.s. (standard deviation 0.5). You select a fish at random. What is the probability that:
 - Its swimming speed is less than 1 m.s.
 - Its swimming speed is greater than 2.5 m.s.
 - Its swimming speed is between 2 and 3 m.s.

Example - 1

- The average swimming speed of a fish population is 2 m.s. (standard deviation 0.5).

You select a fish at random.

What is the probability that:

- It's swimming speed is less than 1 m.s.
= $P(Z < (1-2)/.5) = P(Z < -2) = \mathbf{0.0228}$

Examples-2

- The average swimming speed of a fish population is 2 m.s. (standard deviation 0.5). You select a fish at random. What is the probability that:
 - Is swimming speed is greater than 2.5 m.s.

$$= P(z > (2.5-2)/.5) = P(z > 1) = 1 - P(z \leq 1)$$

$$= \mathbf{0.159}$$

Example-3

- The average swimming speed of a fish population is 2 m.s. (standard deviation 0.5). You select a fish at random. What is the probability that:
 - Its swimming speed is between 2 and 3 m.s.
 - $= P((2-2)/.5 \leq z \leq (3-2)/0.5)$
 $= P(0 \leq z \leq 2) = P(z \leq 2) - P(z \leq 0)$
 $= 0.477$

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End